

DERIVACIÓN

Reglas de derivación

1. $\frac{d}{dx}(c) = 0$
2. $\frac{d}{dx}x = 1$
3. $\frac{d}{dx}(x^n) = nx^{n-1}$ Regla de la potencia
4. $\frac{d}{dx}[c f(x)] = c f'(x)$
5. $\frac{d}{dx}[f(x) + g(x)] = f'(x) + g'(x)$
6. $\frac{d}{dx}[f(x)g(x)] = f(x)g'(x) + g(x)f'(x)$ Regla del producto
7. $\frac{d}{dx}\left[\frac{f(x)}{g(x)}\right] = \frac{g(x)f'(x) - f(x)g'(x)}{[g(x)]^2}$ Regla del cociente
8. $\frac{d}{dx}f(g(x)) = f'(g(x))g'(x)$ Regla de la cadena
9. $\frac{d}{dx}f(x)^n = n f(x)^{n-1} f'(x)$ Regla de la potencia generalizada
10. $\frac{d}{dx}(kx + b) = k f'(kx + b)$
11. $g'(x) = \frac{1}{f'(g(x))}$ donde $g(x)$ es la inversa $f^{-1}(x)$
12. $\frac{d}{dx} \ln f(x) = \frac{f'(x)}{f(x)}$

Funciones trigonométricas

13. $\frac{d}{dx} \sin x = \cos x$
14. $\frac{d}{dx} \cos x = -\sin x$
15. $\frac{d}{dx} \tan x = \sec^2 x$
16. $\frac{d}{dx} \csc x = -\csc x \cot x$
17. $\frac{d}{dx} \sec x = \sec x \tan x$
18. $\frac{d}{dx} \cot x = -\csc^2 x$

Funciones trigonométricas inversas

19. $\frac{d}{dx}(\sin^{-1} x) = \frac{1}{\sqrt{1-x^2}}$
20. $\frac{d}{dx}(\cos^{-1} x) = -\frac{1}{\sqrt{1-x^2}}$

21. $\frac{d}{dx}(\tan^{-1} x) = \frac{1}{1+x^2}$
22. $\frac{d}{dx}(\csc^{-1} x) = -\frac{1}{|x| \sqrt{x^2-1}}$
23. $\frac{d}{dx}(\sec^{-1} x) = \frac{1}{|x| \sqrt{x^2-1}}$
24. $\frac{d}{dx}(\cot^{-1} x) = -\frac{1}{1+x^2}$

Funciones exponenciales y logarítmicas

25. $\frac{d}{dx}(e^x) = e^x$
26. $\frac{d}{dx}(a^x) = (\ln a) a^x$
27. $\frac{d}{dx} \ln |x| = \frac{1}{x}$
28. $\frac{d}{dx}(\log_a x) = \frac{1}{(\ln a) x}$

Funciones hiperbólicas

29. $\frac{d}{dx}(\sinh x) = \cosh x$
30. $\frac{d}{dx}(\cosh x) = \sinh x$
31. $\frac{d}{dx}(\tanh x) = \text{sech}^2 x$
32. $\frac{d}{dx}(\text{csch } x) = -\text{csch } x \coth x$
33. $\frac{d}{dx}(\text{sech } x) = -\text{sech } x \tanh x$
34. $\frac{d}{dx}(\coth x) = -\text{csch}^2 x$

Funciones hiperbólicas inversas

35. $\frac{d}{dx}(\sinh^{-1} x) = \frac{1}{\sqrt{1+x^2}}$
36. $\frac{d}{dx}(\cosh^{-1} x) = \frac{1}{\sqrt{x^2-1}}$
37. $\frac{d}{dx}(\tanh^{-1} x) = \frac{1}{1-x^2}$
38. $\frac{d}{dx}(\text{csch}^{-1} x) = -\frac{1}{|x| \sqrt{x^2+1}}$
39. $\frac{d}{dx}(\text{sech}^{-1} x) = -\frac{1}{x \sqrt{1-x^2}}$
40. $\frac{d}{dx}(\coth^{-1} x) = \frac{1}{1-x^2}$